Fgrctwo gpv'qh' Ekkhlcpf" Eqcuxn Gpi kpggt kpi

f UXi UhY Ghi XYbh < UbXVcc



Herbert Wertheim College of Engineering Engineering School of Sustainable Infrastructure & Environment

UNIVERSITY of FLORIDA

RWTRQUG<

Vj ku'kphqto cvkqp'i wkf g'ku'r tqxkf gf ''q''{qw'kp''qtf gt ''q''koo krkctk g''{qw'y kj "'y g''r tqegf wtgu''cpf 'hqto u'*cmi'r quwgf ''cv' j wr u

j wr u

j wr u

lguulg0whr0gf wlt guqwtegulewttgpv uwwf gpwul-"'y cv'y kmi'dg''wkrkl gf ''f wtkpi "'{qwt "f gi tgg''r tqeguu0J qy gxgt." {qw'uj qwrf "

lktuv'tghgt ''q''{qwt "eqmgi g''ecvcmqi "'cpf ''y g''I tcf wcvg''Uej qqnnu'r qnlekgu''cpf 'r tqegf wtgu''cu''qwrkpgf ''qp''y g''

j wr u

li tcf wcvguej qqn0xhr0gf wl'y gdukg0'Kr'ku'gzvtgo gn('ko r qtvcpv'yj cv''{qw'wpf gtuvcpf ''y gug''r tqegf wtgu''cpf ''o ckpvckp''y g''

r tqeguukpi "'qh''y g''tgs wktgf 'hqto u'kp''c''ko gn(''o cppgt0Cnq. ''dg''egtvckp''yq''tghgt''yq''y g''EEG''F gr ctvo gpv'y gdukg''cv''wpf gt''

y g''j wr u

lguukg0whr0gf wleeg1''I tcf wcvg''rkurkpi ''hqt''y g''o quv'wr/vq/f cvg''kphqto cvkqp0

QWT'O KUUQP'CPF'QDLGEVKXGU<

Vj g'o kukqp"qh''y g'F gr ctvo gpv'qh'Ekxkri'cpf 'Eqcuvcri'Gpi kpggtkpi '*EEG+'ku''vq'dvkrf ''wr qp'c''rgcf kpi 'r tqi tco 'qh'' gzegr vkqpcn'vgcej kpi .''kppqxcvkxg''tgugctej .''cpf 'f gf kecvgf ''ugtxkeg''d{ 'o ckpvckpkpi 'c'untqpi 'ewttkewnwo .''c'j ki j n{ 's wcnkhgf '' cpf ''eqo o kwgf 'hcewn{.''qwuwcpf kpi 'hceknkkgu.''cpf ''guugpvkcn'hwpf kpi ''tgs wktgf ''vq''o ggv'r tqi tco ''pggf u0'Vj g'r tko ct{ '' qdlgevkxg''qh''y g'F gr ctvo gpv'ku'vq'r tqxkf g'yj g'uwf gpv'y kyj ''c'ewttkewnwo 'f guki pgf ''vq''ceeqo r nkuj ''yj tgg'r tko ct{ ''r wtr qugu<

- 30' Vq"r tqxkf g"c"dtqcf "i gpgtcn"gf weckqp"vj cv"gpj cpegu"eqo o wpkeckqp"umkmu"cpf "gpeqwtci gu"cm/ctqwpf "f gxgnqr o gpv" qh"uwxf gpvu. "dqvj "kpf kxkf wcm("cpf "cu"r tqf wevkxg"o go dgtu"qh"uqekgv(.
- 40' Vq"gpuwtg"vj qtqwi j "rtgr ctcvkqp"kp"vj g'hwpf co gpvcnu"qh"uekgpeg"cpf "gpi kpggtkpi ."cpf
- 50' Vq"r tqxkf g"c"hqwpf cvkqp"hqt"vj g"r ncppkpi ."f guki p."eqpuvtwevkqp."cpf "qr gtcvkqp"qh"ekxkti'gpi kpggtkpi "r tqlgew0

Vj g'r tqi tco "cpf "ewttkewnwo "\q"ceeqo r nkuj "\j gug'qdlge\kxgu'r gto k/c'i tcf wcvg'\q"gpvgt'r tce\keg''cpf "eqo o gpeg''nklog/mpi "hgctpkpi "\j tqwi j "r tqhguukqpcn'ce\kxkkgu''qt'i tcf wcvg''uwf kgu0

Vj g'ugeqpf ct { "qdlgevkxg'ku'\q"gpj cpeg"eqpvtkdwkqpu'\q"vj g'Uvcvg. "P cvkqp. "cpf "r tqhguukqp"vj tqwi j "uvtqpi "r tqi tco u'kp" vgcej kpi . 'tgugctej "cpf 'ugtxkeg0

EQOOWPKECVKQP<

Cp{"qhhlekcn'eqo o wpkecvkqp" 'y cv'{qw't gegkxg" htqo "'y g"Wpkxgtukx{ II tcf wcvg" Uej qqnlEqmgi g"qh" Gpi kpggtkpi IF gr ctvo gpv'qh'Ekxkn'cpf "Eqcuvcn'Gpi kpggtkpi "*EEG+"y km'eqo g"vq" {qw'xkc" {qwt" \whnQsf w"g/o ckn'cfftguu0'K'ku" {qwt" tgur qpuklknkx{ "vq"ej gem'y ku"o ckn'tqwkpgn{ "hqt" korqtvcpv'f gcfnkpgu"cpf "eqo o wpkecvkqpu0'Kn'{qw'ej qug"vq"ki pqtg"y ku"hpg"qh" eqo o wpkecvkqp. "kv'eqwnf" korcev'{qw'pgi cvkxgn{ "kp"o cp{ "y c{u"kpenvfkpi "cdrg"vq"i tcf wcvg0}

EJ CRVGT'3<TGI KUVTCVKQP

Qp/'Eco rwu'iwwf gpwi

WHEQWIUG'UEJ GF WNG'? 'i wruzilgpe@wl@f wluge1

WHI TCF WCVG'EQWTUG'F GUETKRVKQP U'? 'Rngcug''xkuk''y g''WHI tcf wcvg''Uej qqn)u'y gdukg''cp \underline{f} 'I tcf wcvg''Ecvenji ''vq''xkgy " y g'Ekxkri'cpf 'Eqcurcn'Gpi kpggtkpi 'I tcf wcvg''eqwtugu''qhhgtgf 0

WHIF KT GEVQT["?" wrudlf ktgevqt { OwhrOrf wl

Eqpicev'kphqto cvkqp'hqt'GUUKG'Cf o kpkintcvqtu."Hcewn("cpf"Uvchh'/"i wr <1/by y y QuulgQvhrQf wlr gqr rg1

Y j gp"{qw'ctg'tgcf {"'q'ugrgev'eqwtugu'ó''r ngcug''pcxki cvg''q''j g"WHEQWTUG''UEJ GF WNG''vq''ugg''y j cv'eqwtugu''y kn'idg''qhhgtgf 0' Vq'hhpf ''qw'o qtg''cdqw'c''ur gekhle''eqwtug''o''{qw''ecp''wug''y g"WHI TCF WCVG'EQWTUG'F GUETKRVKQP U=cnugtpcvkxgn{."{qw''ecp''go cknlecm''y g''hknyf ''kputwevqt''d{''wukpi ''y g"WHF KTGEVQT[0Kt''{qw'y cpvlpggf ''cf xkukpi ''qt''uwi i guvkqpu''o''hggn'htgg''vq'' kps wktg''y kyj ''kpf kxkf wcn'hcewn{''kpvgtguv'qt''{qwt''cecf go ke''cf xkuqt0'I tcf wcvg''ngxgn'eqwtugu''ctg''cny c{u''7222''}

qt"j ki j gt0'Wr "\q'8"etgf ku'ecp"dg"\cmpp"cv\'j g'\wpf gti tcf wcvg"rgxgrl\r tqxkf gf "\j g{ "ctg"rgxgrl\5222"qt"j ki j gt"cpf "qwulkf g"qhl"{qwt" f kuckr rkpg"chwgt '\qdvckpkpi "cr r tqxcrl\r tqo "{qwt 'hcewn\{"cf xkuqt0'W "eqwtugy qtm'O WUV"DG"QWVUKF G"QH"F KUE KRNKP GO

Qp/Eco r wu'Uwf gpv'Tgi kmt cvkqp'Rt qeguu

30'F kuewuu"{qwt "f gi t gg"r rcpu"y ky "{qwt "cf xkuqt "cpf "f gekf g"qp"yi g"eqwtugu"{qw'r rcp"vq"vcng0
40' Uki p"kp"vq"{qwt "OP GOWHGF W'ceeqwpv'cpf "hqmqy "yi g"r t qegf wt gu"r quvgf "hqt "t gi kutcvkqp0
50'Ki"{qw'y kni'pggf "vq"gptqmlkp"cp{"Ekxki'qt"Eqcucn'Gpi kpggtkpi "\$F GRV\$"eqwtugu"cu'yi g{"ctg"hkuvgf "qp"yi g"
\$Uej gf wrg"qh'Eqwtugu\$. "qdvckp"c"GUUG"I tcf wcyg'Eqwtug"T gi kutcvkqp"Hqto "qprkpg"cv'i wr usl!"
y y y QuulkgOwhrQrf wlt guqwtegulewttgpy/uwxf gpwl% ee"wpf gt "EEG"I tcf wcyg'Rtqi tco "hqto uQ

Hqt''y qug''eqwtugu''uj qy p''kp''y g''Rwdrkuj gf ''Uej gf wrg''qh''Eqwtugu''cu''öF GRVö''kv'ku''pgeguuct { ''vq'i gv'y g''uge-kqp'' pwo dgt''htqo ''y g'f gr ctwo gpvt'ygcej kpi ''y g''eqwtug0'Vj g'f gr ctwo gpvt'wug''y ku''u{ uvgo ''vq''eqpvtqri'y cv'uge-kqp''hqt'' c''xctkgv{ ''qh'tgcuqpu.''k0g0''y g''eruukhkec-kqp''gxgri'qh''uwf gpvu.''f guki p''grge-kxg.'y ckkpi ''hqt''y g''qy gt''uge-kqp''q'' hkri'wr .''gve-0'Uki pcwtgu''ctg''tgs wktgf ''htqo ''y g''kpuntwe-vqt''qh''y g''eqwtug''cpf ''y g''uwf gpvyu''ej ckt''qp''y g''I tcf wcyg'' Eqwtug''Tgi kuntc-kqp''Hqto ''vq'tgi kungt''hqt''cpf ''qh''y g''eqwtugu''rkungf ''dgrqy 0

Ekxkn*'EI P'8; 27. 'EI P'8; 32. 'EI P'8; 62. 'EI P'8; 93. 'EI P'8; 96. 'EI P'9; 9; . 'EI P'9; : 2. 'GI P7; 6; " Eqcuven*'GQE'8; 27. 'GQE'8; 56. 'GQE'8; 93. 'GQE. '9; 9; . 'GQE'9; : 2. 'GI P'7; 6;

P qvg<"kp"cf f kkqp"\q"\j g"eqwtugu"huvgf "cdqxg."qvj gt"f gr ctvo gpvu"*klg0"Dwkf kpi "Eqputvevkqp."Gpxktqpo gpvcn"
Gpi kpggtkpi "Uekgpegu."gve0+"wug"\j g"eqpvtqnrgf "ugevkqp"F GRV0Vj g"uwf gpv'o wuv'qdvckp"r gto kuukqp"htqo "vj g"i tcf wcvg"
cf xkuqt "kp"\j g"ur gekhke"f gr ctvo gpv'\q"tgi kuvgt "hqt"\j qug"eqwtugu0

GUUKG'WHGF I G'Uwf gpv'T gi kmt cvkqp'Rt qeguu

WH'GFI G'? "I w u lwhef i g@hr@f wl
WH'GFI G'EQWTUG'NKUV"? "I w u lwhef i g@hr@f wlaprkpg/i tcf.wcw/r tqi tco uleqwtugul
WH'I TCF WC VG'EQWTUG'F GUETKRVKQP U"? "Rrgcug'xkuk'vj g"WH'I tcf.wcwg"Uej qqrnu'y gdukg"cpf "I tcf.wcwg

Ecverii "vq'xkgy "vj g'Ekxkri'cpf 'Eqcuvcri'Gpi kpggtkpi "I tcf.wcvg"eqwtugu'qhhgtgf
WH'F KTGEVQT["? "I w u lif ktgevqt { @hr@f wl

Y j gp"{qw'ctg"tgcf { "vq"ugrgev'eqwtugu"ó"r rgcug"pcxki cvg"vq"j wr udlwhof i g0\hr0f wlqprhog/i tcf wcw/r tqi tco uleqwtugul"vq"ugg" y j cv'eqwtugu"y kni'dg"qhhgtgf 0'Vq"hhof "qw'o qtg"cdqw'c"ur gekhke"eqwtug"ó"{qw'ecp"wug"y g"WHT TCF WC VG"EQWTUG" FGUET KRVKQP U=cnvgtpcvkxgn(."{qw'ecp"go cknlecm'y g"hkurgf "kpurtwevqt"d{ "wukpi "vj g"WHT KTGE VQT[0'Ki"{qw' y cpvlpggf "cf xkukpi "qt"uwi i gurkqpu"ó"hggn'htgg"vq"kps wktg"y kyj "P cpe{ "O eKtcvj ."vj g"GUUKG"GF I G"r tqi tco "eqqtf kpcvqt0" GF I G"uwf gpvu"i gpgtcm{ "vcng"cp{y j gtg"htqo "5"vq"; "etgf kuu"r gt"ugo guvgt0'Uwf gpvu"ctg"pqvkhkgf "xkc"go ckn'cv'yj g" dgi kppkpi "qh'gcej "ugo guvgt"y kyj "ur gekhke"kphqto cvkqp"tgi ctf kpi "vj g"GF I G"r tqi tco "tgi kurtcvkqp0

[qw'y km'y qtm'y kj "yj g'GUUKG'I tcf wcvg'Cecf go ke'Eqqtf kpcvqt'hqt'GUUKG'GFI G'tgi kuvtcvkqp'kuuwgu.'r ngcug'go ckn' GFI G'kps wktkgu''q<<u>'gfi gB guukgOvhrQfw</u>

PQVG<"Vtcpur qtvcvkqp"Ngcf gtuj kr "GFI G"uwf gpvu"uj qwrf "tgcej "qwv"vq"Ft0"Ukxc"Ukxctco cmtkuj pcp"hqt"eqwtug" cf xkugo gpv<u>c"ukxcB eg0vh"uf w</u>

J QNF UXUwf gpwl'eqwf "j cxg"j qrf u'tgi ctf kpi "vj gkt 'tgi kntcvkqp"cpf "vj gwg"y qwf "dg"r qwgf "vpf gt "vj g"uwf gpwl"

OP GOWHGF W ceeqwpv0'Kt'vj gtg"ctg"j qrf u'qpg"uj qwf 'hqrnqy "vj g"kpwtwevkqpu"r qwgf "hqt"gcej "j qrf "vq"j cxg"vj g"j qrf 'tgo qxgf 0'

Ki'c 'tgi kntcvkqp'hqto "ku'uwdo kwgf 'hqt"r tqeguwlpi "cpf "vj g"j qrf "j cu'pqv'dggp"tgo qxgf ."vj g"wchh'o go dgt"y j q"r tqeguwgu"vj g"

hqto "ecppqv'r tqeggf ."vj gtghqtg"vj ku'uj qwrf "dg"ej gengf "r tkqt"vq'uwdo kwkpi "vj g"tgi kntcvkqp'hqto 0

Hwn/who g't gi kmt c wtqp<'Qp/eco r wu'i tcf wcvg''uwwf gpvu''y kyj 'hkpcpekcri'ckf 'pggf ''vq''gptqmikp''; ''etgf kk'j qwtu''kp''yj g''Hcmi'cpf ''
Ur tkpi ''qt'': ''etgf kk'j qwtu''kp''yj g''Uwo o gt0

HipcnVgto 'Tgi kmtcvkqp<F wtkpi ''y g''y to ''y j gp''y g'f gi tgg'ku'cy ctf gf. ''c''uwf gpv'o wuv'dg'tgi knygtgf 'hqt''cv'hgcuv'5''etgf ku'lp'' hcm'qt''urtkpi ''cpf ''4''etgf ku'lp''uwo o gt0'Vj guku'uwf gpvu'o wuv'gptqm'lp'EI P ''qt''GQE'8; 93''cpf ''f qevqtcn'uwf gpvu'o wuv'gptqm''

kp'EIP'qt'GQE'9; : 20Pqp/yi guku'uwf gpvu'o wuv'gptqm'kp''eqwtug''y qtm'yi cv''eqwpvu'\qy ctf''yi g''i tcf wcvg''f gi tgg0'Uwf gpvu'qp''c'' hgmqy uj kr.''vtckpgguj kr.''qt''cuukuvcpvuj kr''o wuv'dg'tgi kungtgf''crrtqrtkcvgn('hqt''yi gkt''crrqkpvo gpvu'0

Ecp'Kdlg'c'rctvwlo g'i tcf wcwg'inwf gpvA'Wprguu''{qw'j cxg'c''ur geldhe'tgi kuntcwlqp'tgs wltgo gpv'd{''y g'i qxgtpo gpv."cp" gzvgtpcn'ci gpe{."qt''y g''wpkxgtukv{"qt"{qwt"cecf go ke'f gr ctvo gpv\%inwej "cu'cp"cuukuvcpvuj kr +:"{qw'o c{'tgi kungt"cu'c''r ctv'vko g" uwwf gpv'ldh''{qw'o ckpvckp''y g''o kpko wo "tgi kuntcwlqp''tgs wltgo gpv'qh''y tgg''etgf kwu'kp''hcm'qt''ur tkpi "cpf "y q''etgf kwu'kp''y g'' uwo o gt0

I tcf wcwg'lwwf gpwl'qp'crrqlpwo gpw'Rrgcug'tgligt''\q"{qwt"qlhgt''rgwgt'lqt''f gvckru''qp''tgi kntcvlqp''tgs wltgo gpwl0[qw'ecp'' ej gem'qp''yj ku''y kyj ''yj g''Rc{tqm'eqpvcev'lqt''{qwt''Uwr gtxkuqt{'Eqo o kwgg'Ej ckt0}

 $\begin{tabular}{l} \label{tabular} \begin{tabular}{l} Eqpf & kmkqp ''K' iy g''uwf gpv't gegkxgu''cp''cf o kmkqp''nywt''y cv't gs wkt gu''ur gekke''eqpf & kkqpu''kp''t ghgt gpeg''vq''i tcf g'' tgs wkt go gpwu''vq''r tqeggf ''y tqwi j ''y g''r tqi tco .''y gp''y g''uwf gpv''uj qwrf 'tgxkgy ''y qug''uvkr wrc kqpu''gcej ''y to ''r tkqt''vq'' gptqmkpi ''hqt''y g''uvdugs wgpv''y to 0'Ki'y g''eqpf & kqp''qh''y ku''ur gekke''eqpf & kqpcn'cf o kmkqp''ku''pqv'o gv.''y g''uwf gpv'y km''pqv'dg'' r gto & kwgf ''vq''uvc{''p''y g''r tqi tco 0} \end{tabular}$

EJ CRVGT'4<FGI TGG'I WAF GNAP GU'CP F'I TCF WCVAQP 'TGS WAT GO GP VU O CUVGTØUF GI TGG'TGS WAT GO GP VU

Rtqi tco u"ctg"f gxgrqr gf "qp"cp"lpf kxlf wcri'dcuku"vq"ucvkuh{ "vj g"uwf gpvzu"r gtuqpcri'pggf u"cpf "ectggt "kpvgtguvu0'Eqpulf gtcdrg" rcvkwf g"ku"r quuldrg"kp"vj g"f gxgrqr o gpv'qhi'qwulf g"kpvgtguvu"vq"uwr r qtv'vj g"o clqt"ctge"qhi'eqpegpvtcvkqp0'Vj ku"kpvgtguv'o c{ "dg" guvcdrkuj gf "kp"i gqrqi {."o cvj go cvleu"cpf "uvcvkurkeu."dwukpguu."qvj gt "dtcpej gu"qh"gpi kpggtkpi ."gve0

Vj g"O cust "qllGpi lpggt lpi "*O G+ff gi tgg"ku"hqt" yj qug"uwf gpwly j q"j cxg"c"dcej gnqtøu"f gi tgg"lp"gpi lpggt lpi "htqo "cp" CDGV"ceetgf lkgf "ewttlewnwo "qt"y j q"j cxg"vcngp 'uwhhelspv'ctvlewrcvlqp"eqwtug"y qtm'vq"o ggv'vj g"o lplo wo "tgs wltgo gpwl" ur gellhlgf "d{"CDGV0Vj g"O cust "qhlUelspeg" "O U+ff gi tgg"lwlhqt" yj qug"uwf gpwl"y lkj "c"pqp/gpi lpggt lpi "wpf gti tcf wcye"f gi tgg" lpystgurgf "lp"vcnlpi "cf xcpvci g"qh'ur gelcnll gf "cf xcpegf "gf wecvlqp" lp"egtvclp" cur gewl"qh'gpi lpggt lpi "cpf" hqt" yj qug"uwf gpwl" y j qug"gpi lpggt lpi "dceecrewt gcye"f gi tgg"lku"pqv'htqo "cp"CDGV"ceetgf lkgf "ewttlewnwo 0

O cungt)u'f gi tagu'ctg'qhhgtaf 'y kij 'c''j guku'qt'pqp/vj guku'qr vkqp0'Vj g''j guku'qr vkqp''tas wktgu'c'o kplo wo ''qh'8''ugo gungt''j qwtu'qh'O cungtøu'tgugctej '*EI P ''qt''GQE'8; 93+0'Vj g''pqp/vj guku'qr vkqp''tas wktgu''c'' o kplo wo ''qh'8''ugo gungt''j qwtu'Qh'TO cungtøu'tgugctej '*EI P ''qt''GQE'8; 93+0'Vj g''pqp/vj guku'qr vkqp''tas wktgu''c'' o kplo wo ''qh'8''ugo gungt''j qwtu'Qhtt''dqvj ''y g''y guku''cpf ''pqp/vj guku'qr vkqpu "cv'ngcuv'37''etgf kuu'o wuv'dg''cv'vj g''i tof wcvg''ngxgn'' cpf 'y kj kp''y g''Ekxkn'cpf ''Eqcuncn'Gpi kpggtkpi 'F gr ctvo gpv."gzennukxg''qh'EI P '8; 93. ''EI P '8; 96''qt''GQE'8; 930'Kp''cf f kkqp." vj g'f gr ctvo gpv'j ki j n(''tgeqo o gpf u''y cv'qpg/vj ktf ''qh'y g''etgf kw''dg''f guki pcvgf ''cu''ōf guki pö0'Vj ku''ku''r ctvkewnctn(''ko r qtvcpv'hqt'' qwt''kpvgtpcvkqpcn'uwnf gpvu'y j q''ctg''pqv'i tcf wcvgu''qh''cp''wpf gti tcf wcvg''CDGV/ceetgf kxgf ''r tqi tco .''cpf 'y j q''ncvgt''o ki j v'uggm''vq'' dgeqo g'tgi kungtgf ''cu''c''Rtqhguulqpcn'Gpi kpggt''*RG+'kp''y g''WUCO'Ej gem'y kij ''{ qwt''cf xkuqt''vq''f gvgto kpg'y j cv''eqwtugu''ecp''dg'' wugf ''vq''o ggv'yj g''f guki p''tgs wktgo gpv0

 $\label{eq:constraint} \textbf{Ki'c''uwf} \ gpv'ku''cy \ ctf \ gf \ ''cp''cuukuvcpwj \ kr .''c''pqp/vj \ guku'O \ cuvgt \not ou'f \ gi \ tgg''r \ tqi \ tco \ ''ku''pqv''cp''qr \ vkqp0'Vj \ g''uwf \ gpv'o \ wuv''eqo \ r \ ngvg''c'' \ vj \ guku'/qr \ vkqp''r \ tqi \ tco \ 0$

Hqt'ITCFWCVIQP'TGSWKTGOGPVU'hqt'gksj gt'vj g'OG'qt'OU'f gi tgg.''tghgt'vq'vj g'ur gekhle'ugevkqp'y ksj kp'vj ku'j cpf dqqm'hqt'vj cv'kphqto cvkqp0

VTCPUHGT'QH'ETGFKV

Qpn("i tcf wcw/rgxgn*7222/9;;;+"y qtm'y kj "c"i tcf g"qh'D'qt"dgwgt."ku"grki kdrg"hqt"tcpuhgt"qh'etgf k0C"o czko wo "qh'37" vtcpuhgt"etgf ku'ctg"cmqy gf 0Vj gug"ecp"kpenwf g"pq"o qtg"y cp"; "etgf ku'htqo "kpunkwwkqpu"crrtqxgf "d{ "WH"y kj "yj g"dcmpeg" qdwckpgf "htqo "pqp/f gi tgg"y qtm'cv'yj g"Wpkxgtukx{"qh'Hrqtkf c0Etgf ku'\tcpuhgttgf "htqo "qyj gt"wpkxgtukkgu"ctg"crrh\gf "\qy ctf" yj g"f gi tgg"tgs wktgo gpvu. "dw'i tcf gu"gctpgf "ctg"pqv'eqo r wxgf "kp"yj g"uwf gpv\u"i tcf g"rqkpv'cxgtci g0Ceegr wpeg"qh'\tcpuhgt"qh" etgf kv'tgs wktgu"crrtqxcn'qh'y g"uwf gpv\u"i tcf wcyg"Uej qqn0

Vj g'tgur qpukdkrkv{ 'tguvu'y kej 'vj g'uvwf gpvøu'cf xkuqt'vq'dcug'ceegr vcpeg'qh'i tcf vcvg'vtcpuhgt'etgf kuu'qp'guvcdrkuj gf "

etksgtkc'hqt"gpuwtkpi 'vj g'cecf go ke'kpvgi tkx{ "qh'eqwtug"y qtn0P q'eqwtugu'vcngp'd{ "eqttgur qpf gpeg"o c{ "dg'wugf 'hqt'i tcf wcvg" etgf kv'qt'vq"o ggv'vj g'tgi kuvtcvkqp'tgs wktgo gpwu'hqt"cp"cuukuvcpvuj kr 0

Vt c pulgt "qliet gf kv'hqt "dqiy "iy g"O cuvgtøu"pqp/yi guku"("iy guku'uwf gpvu'ku't gs wguvgf "iy tqwi j "uwdo kuukqp"qh'c"eqo r ngvgf "O cuvgtøu'Rtqi tco "Rrcp"qh'Uwf { "hqto "hqwpf "j gtg"/"j wr uzlguukg0whr0gf wltguqwtegulewttgpv/uwf gpvu'U'Vj g"r tqi tco "r rcp" kf gpvklygu'iy g'uwf gpvu'ueqwtugy qtm'vq"dg"eqo r ngvgf "iy tqwi j qwv'yi gkt "gpvktg"f gi tgg"r rcp0"Vj gtg"ku'cnuq"cp"ctgc"qp"yi ku'hqto "y j gtg"yi g"ttcpulgt "qh'etgf kv'ecp"dg"kf gpvkltgf 0Qpeg"yi g"hqto "ku'uwdo kwgf "vq"yi g"I tcf wcvg"Cecf go ke'uwchi'vq"dg'r tqeguugf ." yi g"ttcpulgt "qh'etgf kv'tgs wguv'y km'yi gp"dg'uwdo kwgf "vq"yi g"I tcf wcvg"Uej qqn0Uwdo kuukqp"vko ghtco gu'ctg"cu'hqmqy u<

Ocuset øu'pqp/yj guku'/"o kf vgto "qh'yj g'hktuv'ugo guvgt" Ocuset øu''y guku''ó "o kf vgto "qh'yj g'ugeqpf 'ugo guvgt

6-3 <"Vj gtg"ecp"dg"pq<u>"o qtg"vj cp"c"w q/ugo guvgt"i cr</u>"dgw ggp"vj g"eqphgttcri'qh'vj g"dcej grqt)u'f gi tgg"cpf "vj g"hktuv" ugo guvgt"qh'vj g"o cuvgt)u'r tqi tco "kh'6-3"etgf kwu'ctg'vq"dg'tgs wguvgf "vq"dg'vtcpuhgttgf 06-3 'hqto u'eqo r rgvgf 'chvgt "vj g" eqphgttcri'qh'vj g"dcej grqt)u'r tqi tco "ctg"pqv'crrqy cdrg0C"o czko wo "qh"; "etgf kwu'y kri'dg"eqpukf gtgf 'hqt"c"6-3 'vtcpuhgt "qh" etgf kv'tgs wguv'hqt"vj g"Ekxkri'Gpi kpggtkpi "cpf 'Eqcuvcri'('Qegcpqi tcrj ke'Gpi kpggtkpi "rtqi tco 0

Qdvckp"c"eqr {"qh"{qwt"vtcpuetkr w"cpf "f kuewu"y g"vtcpullgt"qh"etgf kw"y ky "{qwt"cf xkuqt0Chgt"{qwt"cf xkuqt"j cu"o cf g" uwi i gurkqpu"cpf "eqo r ngvgf "y g"Rtqi tco "Rncp"qh"Uwf {"hqto ."kv"y km"dg"r tqeguugf "d{"y g"I tcf wcvg"Cecf go ke"Uvchh0C" uwf gpv'o ww'dg"gptqnngf "cv"WH"hqt"y gkt"hlpcn'vgto "qh"gptqnno gpv0Kt"c"uwf gpv'ej qug"vq"gptqnn'cv'cp"qwulf g"kpurkwwkqp"vq"vtcpullgt" eqwtugy qtm"vq"y gkt"f gi tgg"r tqi tco "cv"WH "kv"o ww'dg"eqo r ngvgf "r tkqt"vq"y g"hlpcn'vgto "qh"y g"f gi tgg"r tqi tco 0

Cp"qhhlekcn'tcpuetkr v'htqo "vj g"qvj gt "kpurkwrkqp"o wur'dg"cxckrcdrg"d{"o kf vgto "qh'vj g"ugo guvgt"r tkqt "vq"vj g"uwf gpvau'hlpcn' vgto "hqt"c"tcpuhgt "qh'etgf kv'tgs wguv'vq"dg"eqo r rgvgf "d{"vj g"f gr ct vo gpv0'Vj gt g"y km'dg"pq"gz egr vkqpu'vq "vj ku'cu'cm'vtcpuhgt "etgf ku" o wur'dg'r tqeguugf "cpf "vj qy p"qp"vj g'uwrf gpvau'ttcpuetkr vu'd{"vj g"uwrf gpvau'i tcf wcvkpi "ugo guvgt0

 $Vq''ngctp''o qtg''cdqw''tcpuhgt''etgf kh'tgs wktgo gpwi'cpf''tguwtke klqpu. ''r ngcug''tghgt''q'' y g\underline{''WHI tcf wcwg''Ecvcmji ''} wpf gt'' {qwt'' tgur gevkxg''f gi tgg''r tqi tco 0}$

I tef wevg'Eqwtugu'Vengp'Y j kg'c'Pqp/f gi tgg'lggnkpi 'Uwf gpv

C'Wpkxgtukv("qh"Hnqtkfc"pqp/fgi tgg"uggnkpi "uwwfgpv'y j q"uwdugs wgpvn("ku"cfo kwgf "cpf "gptqmu"kp"I tcf wcvg"Uej qqn'o c{" vtcpuhgt"wr "vq"37"etgf kv"j qwtu"qh"7222"qt"8222"ngxgn'eqwtugu"vcngp0"Vj ku"ku"eqpvkpi gpv'wr qp"cr r tqxcn'qh'vj g"uwwf gpvuø' cf xkuqt"cpf "vj cv'vj g"eqwtugu"o ggv'vj g"o kpko wo "i tcf g"tgs wktgo gpv0

WP KXGTUKV['QH'HNQTKF C'I TCF WCVG'UEJ QQN VTCXGNKPI 'UEJ QNCT'RTQI TCO

Vj ku'r tqi tco 'ku'f guki pgf 'hqt'c'uwf gpv'y j q'y cpwi'q'r ct kekr cvg''cu'c''WH'i tcf wcvg''uwf gpv'cwgpf kpi ''cp'kpurkwwkqp''qh'' j ki j gt''rgctpkpi ''gnugy j gtg. ''gknj gt''y knj kp''nj g''Hqtkf c''Uvcvg''Wpkxgtukx{ ''U{ uvgo ''qt''qwukf g''qh''nj g'''Hqtkf c''Uvcvg''Wpkxgtukx{ ''U{ uvgo ''qt''qwukf g''qh''nj g'''Ypkxgtukx{ ''Ukcvgulo''vj g'''ypkxgtukx{ ''Ukcvgulo''nj g'''ypkxgtukx{ ''Ukcvgulo'''nj g'''ypkxgtukx{ ''Ukcvgulo'''nj g'''ypkxgtukx{ ''Ukcvgulo'''nj g'''ypkxgtukx{ ''Ukcvgulo'''nj g'''ypkxgtukx{ ''Ukcvgulo'''

PQVG<Ki'c'uwf gpv'kı'r wtuwkpi "c'pqp/yj guku'dcugf "f gi tgg"pq'uwr gtxkuqt { "eqo o kwgg'ku'pggf gf ."j qy gxgt''yj g'uwf gpvxu" cf xkuqt¢u'pco g'y km'crr gct'kp''yj g'I KO U'u{ uvgo "cu''yj gkt''ej ckt''*cpf "uj qwrf 'dg''rkuvgf "qp''yj g'r tqi tco "r ncp''cu''yj gkt''ej ckt''cu''y gm+0' Ki'c'pqp/yj guku'uwf gpv'ku'r wtuwkpi "c''o kpqt''ugg''dgmy 0

Ogo dgtuj kr1Crrqkpvo gpv

Uwr gtxkuqt { "eqo o kwggu"hqt"i tef we'y" f gi tgg"r tqi teo u"etg"pqo kpeygf "d { "vj g"tgur gevkxg" f gr etwo gpv'ej ektu." errtqxgf "d { "vj g"eqngi g"f gep"epf "errqkpygf "d { "vj g"F gep"qh'vj g"I tef we'y"Uej qqn0Vj g"F gep"qh'vj g"I tef we'y"Uej qqn1ku"ep" gz/qhhekq"o go dgt"qh'em'uwr gtxkuqt { "eqo o kwggu0Qpn("vj qug"o go dgtu"qh'vj g"heewn{ "y j q"j exg"dggp"errqkpygf "vq'vj g" i tef we'y"heewn{ "o e { "ugtxg"cu"o go dgtu"qh'e"uwr gtxkuqt { "eqo o kwgg"wprguu"e"ur geken'errqkpyo gpv'ku"eqo rngygf "epf" errtqxgf 0Hqt"vj qug'uwwf gpwu"uggmkpi "e"vj guku/deugf "f gi tgg."vj g"eqo o kwgg"o wuv'eqpukuv'qh'e"ej ekt"*htqo "vj g"uwwf gpyzu" j qo g"f gr etvo gpv'o"v{r keem("vj g"ef xkuqt+"epf "epqvj gt"i tef we'y"heewn{ "o go dgt0J qy gxgt."kh'vj g"uwwf gpv'grgevu"vq"r wtuwg"

c'o kpqt"\qy ctf "c"pqp/yi guku"f gi tgg. "yi g"uwf gpv'o wuv'uwdo kb'yi g"eqo r ngvgf "uwr gtxkuqt { "eqo o kwgg"hqto "*ugg"O cungtøu" Rtqi tco "Rncp"qh"Uwf { "hqto +'y kyi "yi g"o kpqt"tgr tgugpvcvkxgøu"pco g"htqo "yi g"f gr ctvo gpv'y j gtg"yi g"o kpqt "y kni'dg"qdvckpgf 0' Vj ku'o wuv'dg"eqo r ngvgf "yi g"ugo gungt "dghqtg"yi g"uwrf gpv'kpvgpf u"vq"i tcf wcvg0"Kii'vy q"o kpqtu"ctg"f guki pcvgf ."vy q" tgr tgugpvcvkxgu"o wuv'dg"cr r qkpvgf "vq"yi g"eqo o kvgg0"Kiic"uwrf gpv'cpvkekr cvgu"o cmkpi "c"ej cpi g"kp"j ku"qt"j gt"i tcf wcvg" eqo o kvgg. "j g"qt"uj g"o wuv'f q"uq"pq"ncvgt"yi cp"o kf vgto "qh'yi g"hkpcn!*i tcf wcvkpi +'ugo gungt0"Vj gtg"ctg"P Q"gzegr vkqpu"vq" yi ku'f gcf nkpg0

Urgekci/Crrqkpvo gpvu

Vj g'uwf gpv'o c{"tgs wguv'ij cv'cp"kpf kxkf wcn'y kyj "ur gekcn's wcnkhecvkqpulgzr gtvkug"dg"c"o go dgt"qh'ij g"eqo o kwgg0Vj g" uwf gpv'o wuv'eqo r ngvg'ij g"oUr gekcn'Uwr gtxkuqt{"Eqo o kwgg"Crrqkpvo gpv'Rgvkxkqpö" **hqwpf "qp'vj g'GUUKG" y gduksg+'cpf "vj g'uwr gpvxu"ej ckt"o wuv'crrtqxg'vj g'hqto 0'Opeg'vj g'hqto "ku'eqo r ngvg."vj g'EEG'I tcf wcvg'tgeqtf u" uvchh'y kmhqty ctf "vj g'tgs wguv'hqt"eqpukf gtcvkqp"d{"vj g'I tcf wcvg'Uej qqn0

I TCFG'RQIPV'CXGTCI G

Cu'r gt 'ý g'WHI tcf wcvg''Uej qqn 'cp{ 'i tcf wcvg''uwf gpv'o c{ 'dg'f gplgf 'hwt y gt 'tgi kutcvlqp'lkh'r tqi tguu'\qy ctf ''eqo r ngvlpi ''ý g'' r tqi tco ''dgeqo gu''wpucvluhcevqt{ ''q''y g''cecf go le''wplx.''eqngi g. ''qt 'F gcp''qh''y g'I tcf wcvg''Uej qqn'0

Wpuckulicevqt { "uej qrctuj kr "ku"f ghkpgf "cu"hcknxtg"vq"o ckpvckp"c"D"cxgtci g"*5022+"kp"cm"y qtm"cwgo r vgf 01 tcf wcvg"uwf gpvu"pggf "cp"qxgtcm"I RC"qh"5022"\twpecvgf "cpf "c"5022"\twpecvgf "I RC"kp"vj gkt "o clqt"*cpf "kp"vj g"o kpqt."kh"c"o kpqt "ku"f genctgf +"cv" i tcf wcvkqp0

Uwf gpvu'y kj ''rguu''y cp'c''5022''I RC''o c{ ''pqv'j qrf ''cp''cuukuvcpvuj kr ''qt 'hgmqy uj kr 0

UVGRU'VQ'HQNNQY 'VQY CTF'I TCFWCVKQP

O CUVGT'\dhGPI KPGGTKPI '\b'PQP/VJ GUKUFGI TGG'TGS WKTGO GPVU

- "" Eqo r rgvg"52"qt"o qtg"etgf kv"j qwtu"*cu"cr r tqxgf "d{"cf xkuqt"cpf lqt"eqo o kwgg+
- "'' O kpko wo "qh'37"etgf kwu'\cngp'kp"o clqt"ctgc
- "" O czko wo "qh'8"etgf ku'qh'\\$5222/6222'hgxgn+'eqwtugu. "qwukf g'lf gr ctvo gpv. "ecp''dg''wugf 'hqt''uwr r qtv'eqwtugu'kh'' cr r tqxgf ''d{ ''cf xkuqt
- "" Cm'y qtm'kpenwf kpi "tcpuhgt "etgf kv."o wuv'dg "eqo r ngvgf "f wtkpi "'y g''ugxgp" { gctu'r tgegf kpi "'y g'' f gi tgg''ku''cy ctf gf
- "" Dg"egtvckp"\j cv'cm'\tcpuhgt"qh'etgf kv'tgs wguwu'y gtg"crrn\gf "\q"{qwt'tgeqtf u'kh"{qw\'uwdo kwgf "c'tgs wguv
- $^{\prime\prime\prime}$ O kpko wo "qh'502" I RC "kp
 "y g''o clqt "ctgc"cpf "ewo wrcvkxg "ku'pggf gf "\q''i tcf wcvg
- "' Vj g'ugo guvgt 'dghqtg'i tcf wcvkqp.''vj g'ecpf kf cvg''uj qwrf ''ej gem<u>il Ko U</u>'vq''o cmg''uwtg''vj gkt''f gi tgg''r tqi tco ''cpf ''vj g''
 Uwr gtxkuqt { ''Eqo o kwgg'kphqto cvkqp''ku''ceewtcvg0
- "" Uwdo k''c <u>"f gi tgg"crrnlecvkqp"</u>d{ "yj g"r quvgf "f gcf nkpg
- \H Cfftguu'r wpkkk
gg'i tcfgu'qp''y g''tcpuetkr vu'y ky ''y g'' I tcfwc
vg''Cecfgo ke''uvchh
- $\label{thm:condition} $$ Tgxkgy "{qwt'eqr { ''qh''y g'Rtqi tco ''Rrcp''qh''Uwf { ''hqto ''vq''dg''egtvckp''{qw''y cxg''o gv''cm''r tqi tco ''tgs wktgo gpvu left for the statement of the state$
- "" Eqo r ngvg" vj g<u>"GUUKG" F gr ct vo gpv" Gz kv" Uwt xg{ "</u>("t gwtp" ng{ u

CNY C[UTGHGT"VQ"VJ G"I TCFWCVG"ECVCNQI "HQT"CNN"QVJ GT"TGS WKTGO GP VU

O CUVGT'QHUEKGPEG'&'PQP/VJ GUKUFGI TGG'TGS WKTGO GPVU

- "Eqo r rgvg'52"qt"o qtg"etgf k/j qwtu'*cu'crrtqxgf "d{ "cf xkuqt"cpf lqt"eqo o kvgg+
- "" O kpko wo "qh"37"etgf ku'\cmgp"kp"o clqt"ctgc
- "" O czko wo "qh'8"etgf ku'qh'*5222/6222"ngxgn+"eqwtugu. "qwukf g'f gr ct vo gpv."ecp"dg'wugf 'hqt'uwr r qt v'eqwtugu'kh' cr r tqxgf 'd{ "cf xkuqt

- "" Cm'y qtm'lpenxf kpi "tcpuhgt"etgf kx."o wuv'dg"eqo r ngvgf "f wtkpi "vj g"ugxgp"{ gctu'r tgegf kpi "vj g"f cvg"qp"y j kej "vj g"f gi tgg'ku"cy ctf gf
- "" Dg"egt vckp" 'y cv'cm' \tcpulgt "qh'etgf kv'tgs wguvu' y gtg"cr r rkgf "\q" { qwt 'tgeqtf u'kh' { qw'uwdo kwgf "c'tgs wguv
- "' O kpko wo "qh"502"I RC "kp" yj g"o clqt" ctgc" cpf "ewo wrcykxg" ku 'pggf gf "\q" i tcf wcyg
- "' Vj g'ugo guvgt'dghqtg'i tcf wcvkqp. 'vj g'ecpf kf cvg'uj qwrf 'ej gem<u>il KOU'</u>vq'o cmg'uwtg'vj gkt'f gi tgg'r tqi tco 'cpf 'vj g' Uwr gtxkuqt { 'Eqo o kwgg'kphqto cvkqp'ku'ceewtcvg0
- "' Uwdo k''c <u>"f gi tgg"cr r rlecvkqp"</u>d{ "yj g"r quygf "f gcf rkpg
- "' Cfftguu'r wpkskxg'i tcfgu'qp'y g'\tcpuetkr uu'y ky 'y g'I tcfwcyg'Cecfgo ke'unchh
- "" Tgxkgy "{qwt'eqr { ''qh''y g''Rtqi tco ''Rrcp''qh''Uwf { ''hqto ''vq''dg''egtvckp''{qw''j cxg''o gv''cm'r tqi tco ''tgs wktgo gpw
- "" O ggv'y kj "{qwt"cf xkuqt "vq"f gvgto kpg"y j gp"vj g"hkpcn'gzco kpcvkqp"tgs wktgo gpv'y km'dg"eqo r ngvgf
- "" Eqo r ngvg'yj g<u>'GUUKG'F gr ctvo gpv'Gzkv'Uvtxg{''</u>("tgwtp''ng{u

CNY C[U'TGHGT''VQ''VJ G'I TCFWCVG'ECVCNQI "HQT'CNN'QVJ GT'TGS WKTGO GP VU

O CUVGT'QHUEKGPEG'&pf'O CUVGT'QHGPI RPGGTRPI '/VJ GURUFGI TGG'TGS WKTGO GPVU

- "" Eqo r rgvg"52"qt"o qtg"etgf kv"j qwtu'*cu"cr r tqxgf "d{ "cf xkrqt"cpf lqt"eqo o kvyg+
- "'' O kpko wo "qh'37"etgf kwu'\cmgp'kp''o clqt''ctgc
- "" O czko wo "qh'8"etgf ku''qh'*5222/6222"hgxgn+"eqwtugu. "qwukf g''f gr ct vo gpv. "ecp''dg''wugf 'hqt''uwr r qt v'eqwtugu'kh'' cr r tqxgf ''d{ "cf xkuqt
- "" Cm'y qtm'kpenwf kpi ''tcpuhgt''etgf kx."o wuv'dg''eqo r ngvgf ''f wtkpi ''y g''ugxgp''{ gctu''r tgegf kpi ''y g''f cvg''qp''y j kej ''y g'' f gi tgg''ku''cy ctf gf
- $\label{eq:constraint} \begin{tabular}{ll} \b$
- $^{\prime\prime\prime}$ O kpko wo "qh'502" I RC "kp
 "y g''o clqt "ctgc"cpf "ewo wrc
vkxg 'ku'pggf gf ''vq''i tcf wcvg
- "" Vj g'ugo gungt 'dghqtg'i tcf wcxlqp. ''y g'ecpf lf cvg'uj qwrf ''ej gem<u>il Ko U'</u>vq''o cmg'uwtg''y glt'f gi tgg'r tqi tco ''cpf ''y g''
 Uwr gtxluqt { 'Eqo o kwgg'lphqto cxlqp'ku'ceewtcvg0
- "" Uwdo k'c<u>"f gi tgg"crrnecwap"</u>d{"yj g"r quvgf "f gcf nkpg
- "'' Cfftguu'r wpkkkg'i tcfgu'qp'yj g'\tcpuetkr vu'y kyj ''yj g'I tcfwcyg'Cecfgo ke'uvchh
- "" Tgxkgy "{qwt 'eqr { "qh' 'y g'Rtqi tco "Rrcp"qh' Uwf { 'hqto '\q'dg'egtvckp" {qw' j cxg' o gv'cm'r tqi tco 'tgs wktgo gpvu
- "' O ggv'y kij "{qwt 'liwr gtxkuqt { "eqo o kwgg" \q"f gvgto kpg" y j gp" \j g"hkpcn"gzco kpcvkqp" tgs wktgo gpv'y km'dg" eqo r ngvgf
- O ggylf gcf rlpg"\q"f gligpf "y g"o cuygtøu"\y guku"cpf "hlpcn'uwdo kuulqp"f gcf rlpg0"Hlpcn'gzco "r cengvu"ctg"nqecvgf "wpf gt" y g"hqto u"hlpm'qp"\y g<u>"GUUlG"\y gdukve</u>0"Hqmqy "\y g"r tqeguu"\y cv'ku"qwrkpgf "\y gtg0\Qpeg"\y g"hlpcn'gzco kpcvkqp"ku" eqo r ngvg. "\y g"crrtqxgf "hqto u"uj qwrf "dg"eqo r ngvgf "r tkqt"\q"\y g<u>"I tcf wcvg"Uej qqn'f gcf rlpgu="</u>qpeg"tgegkxgf ."\y g" I tcf wcvg"Cecf go ke'hvchh'y km'y qtm'qp"kpr wwkpi "{qwt hqto u0
- "" Eqo r ngvg''y g<u>'GUUKG'F gr ct vo_gpv'Gzkv'Uwt xg{ '</u>('t gwtp''ng{ u

CNY C[U'TGHGT''VQ''VJ G'I TCF WCVG'ECVCNQI "HQT'CNN'QVJ GT'TGS WXTGO GP VU

FQEVQT'QH'RJ KNQUQRJ [

Rtqi tco u'ctg'f gxgrqr gf "qp"cp"kpf kxkf wcn'dcuku'\q"uc\kuh{ "\j g"tuwf gpvxu'r gtuqpcn'pggf u'cpf "ectggt "kpvgtguw0' Eqpukf gtcdrg"rc\kwf g"ku'r quukdrg"kp"\j g"f gxgrqr o gpv'qh'qwukf g"kpvgtguwu"\q"uwr r qtv'\j g"o clqt"ctgc"qh'eqpegpvtc\kqp0'Vj ku" kpvgtguv'o c{"dg"guvcdrkuj gf "kp"i gqrqi {."o cvj go cvkeu'cpf "uvc\kurkeu."dwukpguu."qvj gt"dtcpej gu"qh'gpi kpggtkpi ."gve0

Vj g'F qevqt"qhi'Rj krquqr j {"f gi tgg"ku'pqv'f ghkpgf "kp"vgto u'qh'eqwtug"j qwtu'dw'tcvj gt"ku'eqpukf gtgf "vq"eqpukuv'qh'c" hrgzkdrg"r tqi tco "rgcf kpi "vq"o cuvgt {"qhi'c"hkgrf "qh'mpqy rgf i g"cpf "eqpvtkdwkpi "vq"r tqhguukqpcn'f gxgrqr o gpv'vj tqwi j "hqto cn' cpf "kpf gr gpf gpv'uwf {"cpf "tgugctej 0'Kp"cmihkgrf u."vj g"Rj (F 0'f gi tgg"tgs wktgu"cv'rgcuv'; 2"etgf ku'dg{qpf "vj g"dcej grqtøu" f gi tgg"qt "c"o kpko wo "qh'82"etgf ku'dg{qpf "cp"ceetgf kxgf "cpf "cy ctf gf "o cuvgtøu"f gi tgg"hqto cm("f qewo gpvgf "xkc"vj g" O cuvgtøu"F gi tgg"Cempqy rgf i go gpv'*r tqeguu"qwrkpgf "dgrqy +0'C v'rgcuv'67"etgf ku"qh'cp{"f qevqtcn'f gi tgg"o wuv'dg" eqo r rgvgf "cv'vj g"Wpkxgtukv{"qh'Hrqtkf c."cpf "kp"cm'ecugu"y g"uwrf gpv'o wuv'eqo r rgvg"y g"s wcrkh{ kpi "gzco kpcvkqp"cv'vj g" Wpkxgtukv{"qh'Hrqtkf c0

Vj g"r qrle{"qp"\j g"Rgtlqf "qh"Eqpegp\tc\gf"'Uwf {"tgs\wltgo\ gp\'hqt"Rj F\"uwf\ gp\u'j\ cu"dggp"\tgr\ regf\"d{"\j\ g

tgukf gpe{"tgs wktgo gpv"rkuvgf "cdqxg0C"f gr ctvo gpv"qt"eqmgi g"o c{"guvcdrkuj "cpf "o qpkqt"ku"qy p"o qtg"uvtkpi gpv" tgs wktgo gpvu"cu"f guktgf 0"Vj gtg"ku"c"r tgrko kpct{"gzco kpcvkqp"hqt"cm"f qevqtcn"uvvf gpvu"kp"vj g"Ekxkri"Gpi kpggtkpi "O clqt" y j kej "ku"uej gf wrgf "hqt"vj g"uvvf gpvu"ugeqpf "vgto "kp"vj g"r tqi tco 0"Kp"cf f kklqp."cm"f qevqtcn"ecpf kf cvgu"o wuv'ucvkuh{"vj g" hqtgki p"rcpi wci g"tgs wktgo gpv"dghqtg"vcnkpi "vj g"y tkwgp"cpf "qtcn"r qtvkqpu"qh"vj g"s wcrkh{kpi "gzco 0

Vj g'uwr gtxkuqt { "eqo o kwgg"eqpukuwu"qhi'hqwt"r tqhguuqtu0lifo"i gpgtcn"c"o kpko wo "qhi'yi g"ej ckt"cpf "y q"qyi gt"o go dgtu" o wuv'dg'htqo "yi g"F gr ct wo gpv'qhi'Ekxkn'cpf "Eqcuvcn'Gpi kpggtkpi ="kp"cffkkqp."yi g"ej ckt "cpf "qpg"o go dgt"o wuv'dg'htqo "yi g" uwwf gpvxu"o clqt "tgugctej "ctgc0Cmio go dgtu"o wuv'j cxg"c"i tcf wcvg"ercuulkhecvkqp"qhi'I H*I tcf wcvg"Hcewn\{+0Qpg" eqo o kwgg"o go dgt."npqy p"cu"yi g"gzvgtpcn'o go dgt."uj qwnf "dg'htqo "qwukf g"qhi'yi g"f gr ct vo gpv\%dw'uvkm'WHI H+0

 $Gxgt\{ "ecpf kf cvg" hqt"c"f qevqtcn"r tqi tco "ku"tgs wktgf "vq"r tgr ctg"cpf "r tgugpv"c"f kuugt vckqp" yi cv"uj qy u"kpf gr gpf gpv" kpxgurki cvkqp"cpf "ku"ceegr vcdrg" kp"hqto "cpf "eqpvgpv"vq" yi g"uwr gtxkuqt { "eqo o kwgg"cpf "yi g"I tcf wcvg" Uej qqn") Ukpeg"cm" f qevqtcn"f kuugt vckqpu" y km"dg"r wdrkuj gf "d { "o ketqhkro". "kv"ku"pgegurct { "yi cv"yi g"y qtm"dg"qh"r wdrkuj cdrg"s wcrkw{ "cpf "uwkcdrg" kqt"r wdrkeckqp0} }$

Cm'y qtm'hqt''y g'f qevqtcvg''o wuv'dg''eqo r ngvgf ''y ky kp''hkxg''ecngpf ct''{ gctu''chvgt''y g''s wcnkh{ kpi ''gzco kpcvkqp''qt''y ku'' gzco kpcvkqp''o wuv'dg''tgr gcvgf 0

VTCPUHGT'QH'ETGFKV

O cwgt)u'Fgi tgg'Cenpqy rgf i go gpv'*O FC+

 $Cm'eqwtugu''dg \{qpf''y g''o cusetøu''f gi tgg''cmpp''cv'cpqy gt''wpkxgtuk \{''q''dg''cr r rkgf''q''y g''Rj G'Of gi tgg''o ww''dg''cmpp'' cv''cp''kpurkwkqp''qh'hgtkpi ''c''<u>f qevqtcn'f gi tgg</u>''cpf''tgs wktg''cr r tqxcn'qh'y g''Uvr gtxkuqt {''Eqo o kwgg'Ej ckt.'Eqmgi g'F gcp''cpf.''d {''r gkklqp.''y g''I tcf wcy''Uej qqn'qh'y g''Wpkxgtuk {''qh'Hqtkf cOCm''eqwtugu''q'dg''tcpuhgttgf''o ww''dg''ngwgt'' tcf gf.''y ky ''c''I tcf g'' qh'D''qt''dgwgt.''cpf''o ww''dg''f go qpuntcvgf''q'tgrevg'f ktgew {''q''y g''f gi tgg''dgkpi ''uqwi j <math>\psi$ Cm''uwej ''tcpuhgt''tgs wguu''o ww''dg'' o cf g''d {''r gkklqp''pq''rcvgt''y cp''o kf vgto ''qh'y g''y ktf''ugo guvgt''qh''Rj G'Ouwf {OV} g''vqcn''pwo dgt''qh''etgf kwi''kpenwf kpi ''52''hqt''c'' rtkqt''o cuvgtøu''f gi tgg+'y cv'o c {''dg''tcpuhgttgf''ecppqv'gzeggf''67.''cpf''kp''cm''ecugu''y g''uwf gpv'o ww''eqo r rgvg''y g''s wchhl kpi '' gzco kpcvkqp''cv'y g''Wpkxgtuk {''qh''Hqtkf c'lp'' y g''tcf kklqp.''cp{''r tkqt'' tcf wcvg/rgxgn''etgf kwi''gctpgf''cv'y g''Wpkxgtuk {''qh''Hqtkf c'lp'' y g''tco g''f kuekr rkpg''o c {''dg''tcpuhgttgf''kpvq''y g''f qevqtcn''r tqi tco ''cv'y g''f kuetgvkqp''qh'y g''Uvr gtxkuqt {''Eqo o kwggOCp {''r tkqt'' i tcf wcvg/rgxgn''etgf kwi''gctpgf''cv'y g''Wpkxgtuk {''qh''Hqtkf c''kp'' c''f khfvgtgyv'f kuekr rkpg''o c {''dg''tcpuhgttgf''kpvq''y g''f qevqtcn'' rtqi tco ''cv'y g''f kuetgvkqp''qh'y g''f kuetgvkqp''qh'y g''f tecugu.''kv'ku''guugpvkcn'' y cv'y g''f kketgvkqp''qh'y g''f gi tgg''r tkykqp''q''y g''f gi tgg''r tgugpvl ''dgkpi ''uqwi j v0'''y cv'y g''f gi''y gryccpeg''qh'y g''r tkyt''eqwtug'y qtm'y g''f gi tgg''r tgugpvl ''dgkpi ''uqwi j v0''''y g'''y g'''

Kic'uwf gpvif gelf gu'vq'gptqm'cpf 'eqo r ngvg'c'eqwtug'cv'cp'qwulf g'lpurkwwlqp'vq'vtcpuhgt'eqwtugy qtm'vq'y glt'f gi tgg'' r tqi tco "cv'WH 'kv'o wuv'dg'eqo r ngvgf 'r tlqt'vq'y g'hlpcn'vgto "qh'y g'f gi tgg'r tqi tco 0°Cp'qhhlekcn'vtcpuetlir v'htqo "y g'qy gt" lpurkwwlqp'o wuv'dg''cxckrcdng''d{"o kf vgto "qh'y g'ugo guvgt'r tlqt'vq''y g'uwf gpvau'hlpcn'vgto "hqt'c'vtcpuhgt'qh'etgf kv'tgs wguv'vq''dg'' eqo r ngvgf "d{"y g'f gr ctvo gpv0'Vj gtg'y km'dg'pq'gzegr vlqpu'vq''y ku'cu'cm'vtcpuhgt''etgf ku''o wuv'dg''r tqeguugf "cpf "uj qy p'qp''y g'' uwf gpvau'vtcpuetlir vu''d{"y g'uwf gpvau''i tcf wcvlpi 'ugo guvgt0'Vj g''vtcpuhgt''etgf ku''o wuv'dg''nkuvgf 'qp''y g''uwf gpvau''Rj F 'Rtqi tco "Rncp'qh''Uwf {'hqto "cpf "cr r tqxgf 'd{"y g'uwf gpvau''y g'' let'hqt'y g''EEG'I tcf wcvg''tgeqtf u'uvchh'vq''r tqeguu'c''tgs wguv'vq'' y g'I tcf wcvg''Uej qqn'hqt''eqpuhf gtcvkqp''p*q'invyt''y g''y g''o kf/r qlpv'qh'y g''Rj F 'lwwf gpvau'y kf f' vgt o "qh'gpt qmo gpv*0

Vj g'tgur qpukdkrk/{ 'tguwi'y kij ''y g'uwr gtxkuqt { 'eqo o kwgg''vq'dcug'ceegr wpeg''qh'i tcf wcvg''tcpuhgt''etgf kwlOFC'' tgs wguwi'qp''guwcdrkuj gf ''etkgtkc'hqt''gpuwtkpi ''y g''cecf go ke''kpvgi tkx/{ "qh''eqwtug''y qtm0Pq''eqwtugu''vcmgp''d{ ''eqttgur qpf gpeg'' o c{ "dg''wugf 'hqt''i tcf wcvg''etgf kx'qt''vq''o ggv''y g''tgi kntcvkqp'tgs wktgo gpwi'hqt''cp''cuukuvcpwij kr 0

:

Vq"rgctp"o qtg"cdqwv"tcpuhgt"etgf kv"tgs wktgo gpvu"cpf "tguvtkevkqpu."r rgcug"tghgt"vq"vj g<u>"WHI tcf wcvg"Ecvcmji</u> wpf gt"{qwt" tgur gevkxg"f gi tgg"r tqi tco 0

I tcf wcvg'Eqwtugu'Vcmgp'Y j krg'c'Pqp/f gi tgg'Uwf gpv

C''Wpksgtuk ("qh'Hrqtkfc'pqp/f gi tgg'uggnkpi 'uwf gpv'y j q'uwdugs wgpvn ("gptqmu'kp'I tcf wcvg''Uej qqn'o c { 'vtcpuhgt'wr 'vq'' 37''etgf kv'j qwtu'qh'7222''qt'8222''ngxgn'eqwtugu'vcngp0'Vj ku'ku'eqpvkpi gpv'wr qp''cr r tqxcn'qh''y g''uwf gpvou''cf xkuqt''cpf 'vj cv'yj g'' eqwtugu'o ggv'yj g'o kpko wo 'i tcf g'tgs wktgo gpv0

WP KXGTUKV['QH'HNQTKF C'I TCF WCVG'UEJ QQN" VTCXGNKPI 'UEJ QNCT'RTQI TCO

Vj ku'r tqi tco 'ku'f guki pgf 'hqt'c'uwf gpv'y j q'y cpwi'vq'r ctvkekr cvg'cu'c''WH'i tcf wcvg'uwf gpv'cwgpf kpi ''cp'kpurkwkqp''qh'' j ki j gt'ngctpkpi ''gnugy j gtg. ''gkvj gt''y kyj kp''y g''Hqtkf c''Ucvg''Wpkxgtukv{ ''U{ uvgo ''qt''qwukf g''qh''y g''Hqtkf c''Ucvg''Wpkxgtukv{ ''U{ uvgo ''q'twyb kyj kp''y g''Wpkxgf ''Ucvgu0'Vj g''hqto ''vq''tgs wguv'r ctvkekr cvkqp''kp''y ku'r tqi tco ''ecp''dg''hqwpf ''cv<u>cvvtcxgrkpi ''</u> Uej qret'Hqto 0

UWRGTXKUQT['EQO O KVVGG'KPHQTO CVKQP

Crrqlpvo gpv

Ogo dgtuj kr

Vj g''Rj (F 0'Uwr gtxkuqt { "Eqo o kwgg''uj qwrf "dg''eqo r ngvgf "d{ ''yj g''o kf r qlpv''qh''yj g''yj ktf ''ugo guvgt ''qh''tgi kuntcvkqp0'Vj g'' i gpgtcn'lf wkgu''cpf ''tgur qpukdkrkkgu''qh''yj g''Uwr gtxkuqt { 'Eqo o kwgg''hqt ''yj g''f qevqtcn'ecpf kf cvg''ctg''f guetkdgf ''kp''yj g''I tcf wcvg'' Ecwcnji 0'Vj g''Uwr gtxkuqt { 'Eqo o kwgg''eqpukuvu''qh''hqwt''o go dgtu''ugrgevgf ''htqo ''yj g''i tcf wcvg''hcewn{0'Cv''ngcuv''y q''o go dgtu.'' kpenwf kpi ''yj g'Ej ckt.''o wuv''dg''htqo ''yj g''uwrf gpvxu''j qo g''f gr ctvo gpv.''cpf ''cv''ngcuv''qpg''o go dgt''o wuv''dg''htqo ''c''f khfrgtgpv'' f gr ctvo gpv''q''ugtxg''cu''yj g''gzvgtpcn'o go dgt0

UrgekchCrrqkpvo gpvu

Vj g'uwf gpv'o c{ 'tgs wguv'y cv'cp'kpf kxkf wcri'y kj ''ur gekcri's wcrkhecvkqpulgzr gtvkug'dg'c'o go dgt''qh''y g'eqo o kwgg0' Vj g'uwf gpv'o wuv'eqo r ngvg''y g''ōUr gekcri'Uwr gtxkuqt { ''Eqo o kwgg'Crrqkpvo gpv'Rgvkkqpö' \mathfrakqppf ''qp''y g''GUUKG''v gdukgg+'' cpf ''y g'uwf gpvou'ej ckt'o wuv'crrtqxg''y g'hqto 0Qpeg''y g'hqto ''ku'eqo r ngvg.''y g''EEG'I tcf wcwg'tgeqtf u'uvchi'y kmihqty ctf ''y g'' tgs wguv'hqt'eqpukf gtcvkqp''d{ ''y g''I tcf wcwg''Uej qqrf)

I TCFG'RQIP V'CXGTCI G

Cu'r gt''y g'WHI tcf wcyg''Uej qqn"cp{'i tcf wcyg''uwf gpv'o c{"dg'f gpkgf 'hwtyi gt'tgi kuxtcykqp'khir tqi tguu'vqy ctf 'eqo r ngykpi ''y g'' r tqi tco ''dgeqo gu''wpucykuhcevqt{"vq'yi g''cecf go ke''wpkx''eqmgi g."qt'F gcp''qh''y g''I tcf wcyg''Uej qqn0

Who was the control of the control o

cp"qxgtcm'I RC"qh'5022"\twpecvgf "cpf "c"5022"\twpecvgf "I RC"\kp"\yj g\k"o clqt"\cpf "\kp"\yj g\o kpqt."\kh'c"o kpqt '\ku'f genctgf +"cv" i tcf wc\kqp0

Uwf gpul'y kj 'rguu'y cp'c'5022'I RC'o c{ 'pqv'j qrf 'cp'cuukucpuj kr 'qt 'hgmqy uj kr 0

NGCXG'QH'CDUGPEG'RQNÆ[

Vj g'I tcf wcvg'Eqwpekn''cv'vj gkt''O c{''3: .''3; :; .''o ggvkpi .''cf qr vgf ''c'Ngcxg''qh'Cdugpeg''Rqrke{''hqt''cm'f qevqtcn'uwf gpvu0' Vj g''r qrke{''cu'hqrmqy u''dgeco g''ghhgevkxg''Hcm'Ugo guvgt''3; :; 0

õC "f qevqtcn'uwf gpv."y j q"y km'pqv'dg"t gi kuvgt gf "cv'vj g"Wpkx gt ukv{ "qh'Hnqt kf c"hqt "c"r gt kqf "qh'o qt g"vj cp"qpg"
 ugo guvgt. "pggf u"vq"t gs wguv'y tkwgp"r gto kuukqp"ht qo "j kulj gt "hcewnv{ "cf x kuqt "hqt "c "rgcxg"qh'cdugpeg"hqt "c"f guki pcvgf "r gt kqf "qh'vko g0o

Vj tgg"ugo guvgtu"qh"eqpugewkxg"pqp/gptqmo gpv"y km"tguvm"kp"f kueqpvkpvcvkqp"qh"c"r tqi tco "cpf "vj g"uvwf gpv"y km" pggf "vq"uvvdo kv"c"tgcf o kuukqp"i tcf wcvg"cr r necvkqp"vq"dg"eqpukf gtgf "ci ckp"hqt"tgcf o kuukqpu"vq"vj gkt "uco g"r tqi tco 0

TGUGCTEJ 'RTQRQUCN

Vj g"f qevqtcn'uwf gpv'o wuv'r tgr ctg"cpf "r tgugpv'c"y tkwgp"f qevqtcn'tgugctej "r tqr qucn"f gxgnqr gf "kp"eqpuwwcwkqp"y kj "vj g" Uwr gtxkuqt { "Eqo o kwgg"Ej ckt."vq"vj g"Uwr gtxkuqt { "Eqo o kwgg0Vj g"f qevqtcn'uwvf gpv'o wuv'vj gp"o cng"cp"qtcn'r tgugpvcwkqp"qh" vj g"r tqr qucn'vq"vj g"Uwr gtxkuqt { "Eqo o kwgg"r tkqt"vq"vj g"s wcnkh{kpi "gzco kpcwkqp0

S WCNHI IPI 'GZCO

Y tkwgp"cpf "qtcn"eqo r tgj gpukxg"s wcrkh{kpi "gzco kpckqpu"ctg"tgs wktgf "qh"cm"Rj (F 0'ecpf kf cvgu0'Vj g"gzco u"uj qwrf "dg" vcmgp"pq"rcvgt"vj cp"vj g"hqwtyi "ugo guvgt"qh"tgukf gpeg"vqy ctf "vj g"f gi tgg0'Vj g"Uwr gtxkuqt { "Eqo o kwgg"j cu"hwn" tgur qpukdkrkv{ "hqt"vj g"hqto wrcvkqp."cf o kpkutcvkqp."cpf "gxcnwcvkqp"qh"vj g"s wcrkh{kpi "gzco 0Cttcpi go gpwu"nqt"vj g"gzco "uj qwrf "dg"o cf g"kp"eqpuwncvkqp"y kyj "vj g"Uwr gtxkuqt { "Eqo o kwgg"Ej ckt0'Y j gp"{qw"ctg"tgcf { "vq"uej gf wrg"{qwt"qtcn" f ghgpug."{qw"o wuv"eqo r rgvg"vj g"qp/rkpg"Cf o kuukqp"vq"Ecpf kf ce { "hqto "cvz"j wruz|lguukg0xhr0zf wttguqwtegulewttgpv" uwwf gpwu]

CFOKUKQP'VQ'ECPFKFCE[

C"i tcf wcy"uwf gpv"f qgu"pqv'dgeqo g"c"ecpf kf cvg"hqt"yj g"Rj (F 0f gi tgg"wpvkrli tcpvgf "hqto cn'cf o kuulqp"vq"ecpf kf ce $\{0$ Uwej " cf o kuulqp"tgs wktgu"yj g"cr r tqxcn'qh''yj g"uwf gpvwø"Uwr gtxkuqt $\{$ "Eqo o kwgg(0Vj g"cr r tqxcn'y kn'idg"dcugf "qp" $^{18}3+^{1}$ yj g"cecf go ke" tgeqtf "qh''yj g"uwf gpv." $^{14}4+^{1}$ yj g"qr kpkqp"qh''yj g"Uwr gtxkuqt $\{$ "Eqo o kwgg"eqpegtpkpi "qxgtcm'hkxpguu'hqt"ecpf kf ce $\{$." $^{18}5+^{1}$ cp" cr r tqxgf "f kuugt vc.kqp"vqr ke."cpf " $^{18}6+^{1}$ uweeguuhwrieqo r ng.kqp"qh'c"s wcnkh $\{$ kpi "gzco kpc.kqp"cu"f guetkdgf "cdqxg(0Cf o kuulqp"vq" ecpf kf ce $\{$ "y kn'idg"o cf g"cu'uqqp"cu''yj g"s wcnkh $\{$ kpi "gzco kpc.kqp"j cu'dggp"r cuugf "cpf "c"f kuugt vc.kqp"vqr ke'j cu'dggp"cr r tqxgf "d $\{$ "yj g"uwwf gpvwø'Uwr gtxkuqt $\{$ "Eqo o kwgg(0Qpeg"cr r tqxgf ."yj g"Cf o kuulqp"vq"Ecpf kf ce $\{$ "hqto "y kn'idg"y qtngf "qp"d $\{$ "yj g"Cecf go ke"Qhileg"hqt"uwdo kuulqp"vq"yj g"I tcf wcvg"Uej qqn(0)

VKO G'NKO KVU

Vj g'Rj (F 0f gi tgg'o wuv'dg'eqo r ngvgf 'y ky ky ky 'hkxg'ecngpf ct''{ gctu'chygt 'r cuukpi ''y g''s wcrkh{ kpi ''gzco .''qt''y ku''gzco ''o wuv'dg'' tgr gcvgf 0'Cv'ngcuv'y q''ugo guvgtu''o wuv'grcr ug''dgwy ggp''cf o kuukqp''vq''ecpf kf ce{ "cpf "vj g'f cvg''qh'vj g''cy ctf kpi ''qh'vj g'f gi tgg0' Vj g''ugo guvgt ''kp''y j kej ''y g''s wcrkh{ kpi ''gzco ''ku''r cuugf ''ku''eqwpvgf ''kh'vj g''gzco ''ku''eqo r ngvgf ''r tkqt ''vq''y g''o kf/r qkpv''qh'vj g'' ugo guvgt0

HIP CN'GZCO

Wr qp"eqo r ngvkqp"qh"yj g"f kuugt vcvkqp."yj g"Uwr gtxkuqt { "Eqo o kwgg"y km"eqpf wev"c"hpcn"qtcn"gzco kpcvkqp. "hqewugf" r tkpekr cm{ "qp"yj g"f kuugt vcvkqp"tgugctej ."cmj qwi j "qyj gt"tgngxcpv"vqr keu"o c{ "cnuq"dg"gzco kpgf 0"Vj g"gzco kpcvkqp"ecp"dg" uej gf wrgf "f wtkpi "yj g"ygto "r tqeggf kpi "yj g"ugo guvgt"kp"y j kej "yj g"f gi tgg"ku"vq"dg"eqphgttgf 0"Uwf gpvu"ctg"tgur qpukdng"hqt" eqqtf kpcvkpi "y kyj "yj gkt "Eqo o kwgg"O go dgtu"vq"uej gf wrg"yj g"ko glf cvg"qh"yj gkt "gzco 0"Vj g"hkpcn"gzco "r cengvu"ctg"nqecvgf "wpf gt"yj g"hqto u"hpn"qp"yj g<u>"GUUKG"y gdukvg0"Hq</u>mqy "yj g"r tqeguu"yj cv'ku"qwvkpgf "yj gtg0Qpeg"yj g"hkpcn"gzco kpcvkqp"ku" eqo r ngvg. "yj g"crr tqxgf "hqto u"uj qwrf "dg"eqo r ngvgf "r tkqt"vq"yj g<u>"Ltcf wcvg"Uej qqn"f gcf rkpgu="</u>qpeg"tgegkxgf. "yj g"Ltcf wcvg"

Cecf go ke'uvchh'y km'y qtm'qp'kpr wwkpi "{qwt'hqto u0

FKUGTVCVKOP'UWDO KUKOP

I wkf grkpgu''eqpegtpkpi "vj g<u>"hqto cv'qhi'vj g"f kuugtvcvkqp"</u>cpf "grgevtqpke"twdo kuukqp"tgs wktgo gpvu''ctg"r wdrkuj gf "d{ "vj g" I tcf wcvg"Uej qqrlGf kqtkcrlQhhleg0Cp{ "s wgwkqpu'tgi ctf kpi "vj ku'uj qwrf "dg"f ktgevgf "vq"vj g<u>"Gf kqtkcrlQhhleg0</u>Cnuq"pqvg"vj cv" yj g"WO KRt qs wgw'Rwdrkuj kpi "Ci t ggo gpv'tuj qwrf "dg"qdvckpgf "htqo "vj g"Gf kqtkcrlQhhleg0

UVGRUVQ'HQNNQY 'VQY CTF'I TCFWCVKQP'hqt'\j g'RJ F

- "" Eqo r rgvg"; 2"qt"o qtg"etgf kv"j qwtu'*cu'cr r tqxgf "d{ "cf xkuqt"cpf lqt"eqo o kwgg+
- "" O kpko wo "qh"37"etgf ku'\cmgp"kp"o clqt"ctgc
- "" O czko wo "qh'8"etgf ku"qh'*5222/6222"hgxgn+"eqwtugu."qwukf g'f gr ct vo gpv."ecp"dg'wugf 'hqt'uwr r qt v'eqwtugu'kh' cr r tqxgf "d{"cf x kuqt
- "" Cm'y qtm'kpenwf kpi "\tcpuhgt"etgf kx."o wuv'dg"eqo r ngvgf "f wtkpi "vj g"ugxgp"{gctu'r tgegf kpi "vj g"f cvg"qp"y j kej "vj g"f gi tgg"ku"cy ctf gf
- "" Dg"egt vckp" 'yj cv'cm' \tcpuhgt "qh'et gf kv't gs wguwu' y gt g"cr r rkgf "\q" { qwt "t geqt f u'kh" { qw'uwdo kwgf "c't gs wguw
- "' O kpko wo "qh"502"I RC "kp" yj g"o clqt" ctgc" cpf "ewo wrcykxg" ku" pggf gf "\q"i tcf wcyg
- Eqorgyg'yj g'y tkwgp'cpf 'qtcn's werkh{kpi "*Cfoky'vq'Ecpfkfce{+'gzco
- "" Cfftguu'r wpkskxg'i tcfgu'qp'y g'\tcpuetkr wi'y kj ''y g'I tcfwcyg'Cecfgo ke'uwchh
- "' Uwdo ki'c<u>"f gi tgg"crrnecvkap"</u>d{"'yj g"rquvgf "f gcfnkpg
- "Á Tgxkgy "{qwt 'eqr { "qh' y g' Rtqi tco "Rrcp"qh' Uwf { 'hqto "vq"dg"egtvckp" {qw' j cxg 'o gv'cm'r tqi tco 'tgs wktgo gpw
- "Á Vj g'ugo guvgt "dghqtg"i tcf wcvkqp. "vj g'ecpf kf cvg"uj qwrf "ej gem<u>il Ko U</u>vq"o cmg"uwtg"vj gkt "f gi tgg"r tqi tco "cpf "vj g"
 Uwr gtxkuqt { "Eqo o kwgg"kphqto cvkqp"ku"ceewtcvg0
- "" Uwdo k/cp"crrtqxgf "Vtcpuo kwcnl'gwgt" eqpvcev<u>"i tcfqhhlegB guukg(whrl)gfw'</u>hqt" y ku'f qewo gpv+
- "" Oggv<u>iht uv'uwdo kuukap "f gcf rkpg</u>
- O ggv'y kj "{qwt'uwr gtxkuqt { "eqo o kwgg"\q"f gvgto kpg"y j gp"\j g"hkpcn'gzco kpc\kqp"tgs wktgo gpv'y km'dg"eqo r ngvgf "cpf "r tqeguu'\j g"r cr gty qtm
- "' F ghgpf 'vj g'Rj F 'cpf 'o ggv'vj g'hkpcn'uwdo kuukqp'f gcf nkpg
- "Á Uwdo ki WO K'Rtqs wguv hato "va <u>"Gf katken ahhee</u>
- "" Eqo r ngvg'y g<u>'GUUKG'F gr ctvo gpv'Gzkv'Uwtxg{"</u>("tgwtp"ng{u

CNY C[U'TGHGT''VQ''VJ G'I TCFWCVG'ECVCNQI 'HQT'CNN'QVJ GT'TGS WKTGO GP VU

EJ CRVGT'5<'CECFGO KE'J QPGUV['CPF'EQFG'QHEQPFWEV

WPKXGTUKV['RQNKE['QP'CECFGOKE'J QPGUV[

J QPQT'EQFG

 $\label{thm:colorport} \begin{tabular}{l} k had color of the color of$

Rt gco drg<

 $\label{thm:continuous} \begin{tikzpicture} \$

 $Vj\ g'J\ qpqt'Eqf\ g'kl'\delta'$ $\delta Y\ g$. " $i\ g''$ g'' g''

Rugf i g<Qp"cm"y qtm"uwdo kwgf "hqt"etgf kv"d { "uwf gpw"cv"y g"Wpkxgtukk { "qh"Hnqtkf c." y g"hqmqy kpi "r ngf i g"ku"gky gt" tgs wktgf "qt"ko r nkgf " ~oQp"o { "j qpqt." Kj cxg"pgky gt"i kxgp"pqt"tgegkxgf "wpcwy qtk gf "ckf"kp"f qkpi "y ku" cuuki po gpvlo

EJ CRVGT'6<'HIP CPEICN'O CVVGTU

S werkhligf "i tef wevg"uwif gpvu"etg"grki kdrg"hqt"euukuvepvuj kr u"epf "qvj gt"hkpepeken"ey etf u0"Uwif gpvu"etg"gpeqwtei gf "vq" ur gem"y kij "vj g"heewnik "eqpegtpkpi "tgugetej "r tqlgevu"epf "euukuvepvuj kr u0"

NGVVGTUQH'QHHGT'CPF'CRRQIPVO GPV

Y j gp"{qw'j cxg"dggp"cy ctf gf "cp"cuulurcpuj kr."c"ngwgt"qh'qhhgt"y km'dg"i kxgp"\q"{qw0Vj ku'o wuv'dg'uki pgf "cpf" tgwtpgf "\q"\j g"f gr ct vo gpv'hqt"r tqeguulpi 0[qw'y km'y gp"tgegkxg"c"Ngwgt"qh'Crrqkpvo gpv0Vj ku'ngwgt "eqpvckpu'y g" f guetkr vkqp"qh'y g"i tcf wcyg"cuulurcpvu'ucnet {."ghhgevkxg"f cvgu'qh'crrqkpvo gpv."uwr gtxkuqt"cpf "lqd"f wkgu0Vj g"Ngwgt"qh' Crrqkpvo gpv'o wuv'dg'uki pgf "d{"y g"lwr gtxkuqt"cpf "uwf gpv0Vj g"crrqkpvo gpvu"ctg"uwdo kwgf "d{"y g"kpuntwevkqp"qh'y g" hcewn{"o go dgt0Kh'y gtg'ku'cp"gttqt"kp"y g"Ngwgt"qh'Crrqkpvo gpv."r ngcug"pqvkh{"GUUKG"J T"uvchh'uq"y g{ "ecp"ej geniqp"kv" cpf "o cmg"cp{"pgeguuct{"ej cpi gu0}

UN P'WR'HQT'RC[TQNN

Ko"qtf gt "vq"tgegkxg"c"r c{ej gem"{qw'o wuv'dg"uki pgf "w "qp"r c{tqm0GUUKG"J T"uvchh'y km'ugpf "{qw'cp"go ckriy kyj " kpuntwevkqpu'tgi ctf kpi "tgs wktgf "j ktg"f qewo gpvu"cpf "cevkqpu0Vj g"tgs wktgf "f qewo gpvu"kpenwf g"c"WUUuqekcn'ugewtkx{"ectf 0' Kovgtpcvkqpcn'uwf gpvu"y kyj qw'c"uqekcn'ugewtkx{"ectf "y km'dg"i kxgp"c"ygo r qtct{"pwo dgt"cpf "y km'gxgpwcm{"pggf "vq"cr r n{" hqt"qpg0

VWWKOP'Y CKXGT'CPF'HGGU

[qwt'wkklqp'y km'dg'r ckf 'hqt'; 'ugo guvgt'etgf kv'j qwtu'kp''y g'Hcm'cpf ''Ur tkpi .'8' kp''y g''Uwo o gt0[qwt'wkklqp'y ckxgt'' y km'twp''chvgt'F tqr ICff 0[qw''ctg'tgur qpuklrg'hqt'r c{kpi "{qwt'hggu''y cv'ecp''dg''xkgy gf "cv<u>'j wr uslehq0whr@f whrwf gpv'' hbcpekcn'tguqwtegulewttgpvcpf/hqto gt/uwf gpw14247/48/cecf go ke/{gct/wkklqp/cpf/hggul'0'Vj gtg'o c{''dg''c'f grc{''hp''y g'' r tqeguukpi "qh''{qwt''wkklqp''y ckxgt''uq''r c{"c''uo cmi'co qwpv'qh''hggu''dghqtg''y g'f gcf nhpg0'Hcknwtg''vq''o ggv''y gug''f gcf nhpgu'' eqwrf 'tguwnv'kp''{qw''dgkpi 'ej cti gf ''c''8322022'hcvg''hgg0</u>

Vwkkqp'y ckxgtu'y kni'dg''xqkf gf 'kh''y g''cr r qkpvo gpv''vgto kpcvgu''dghqtg''y g''gpf ''qh''y g''ugo guvgt. ''qt''y g''uwwf gpv'' y ky f tcy u'htqo ''y g''Wpkxgtukv{0'Kt''y g''wkkkqp''y ckxgt''ku''xqkf gf . ''y g''uwwf gpv'ku''t gur qpukdrg''hqt''y g''gpvktg''co qwpv''qh''wkkkqp'' cpf 'hggu0

GXCNWCVKQPU

Ki'ku'tgs wktgf ''d{ ''y g'I tcf wcvg''Uej qqri'yi cv'cp{ ''uwf gpv'j qrf kpi ''cp''cuukuvcpwij kr ''j cxg''c'Iqd''r gthqto cpeg''gxcnwcvkqp'' f wtkpi ''yi g'eqpvtcev'r gtkqf ''cu''uvcvgf ''kp''yi g'Ngwgt''qh''Cr r qkpvo gpv0'Uwf gpwi'cpf ''hcewn{ ''uwr gtxkuqtu''ctg'tgs wktgf ''vq''uki p'' yi g'r gthqto cpeg''gxcnwcvkqp''cpf ''tgwtp''vq''GUUKG'J T0

IP VGTP CVKQP CN'UVWF GP VU

Ki'{qwt''xkuc''gzr ktgu.''wpf gt''pq''ektewo uvcpegu''ecp''{qw'dg''r ckf ''pqt''ecp''{qw'j cxg''c''wkkqp''hgg''y ckxgt0'Kpvgtpcvkqpcn'' uwf gpwi'j qnf kpi ''cp''H'3''xkuc''o c{ ''pqv'y qtm'o qtg''y cp''c''vqvcn'qh'42''j qwtu''r gt''y ggn0'Vj ku'ku''y g''vqvcn'qh'cm'cr qkpvo gpw0'' Kp''cf f kkqp.''uwf gpwi'j qnf kpi ''cp''H'3''xkuc''o c{ ''pqv'y qtm'qhh'eco r wv0

EJ CRVGT'7<'UCHGV[

Vj g"xctkqwu"redqtevqtkgu"qr gtevgf "d{ "vj g"f gr etvo gpv"ctg"j c| ctf qwu"y qtmkpi "etgeu#Vj g"F kxkukqp"qh"Gpxktqpo gpven" J genij "epf "Uchgv("qh"vj g"Wpkxgtukv("qh"Hrqtkf e"r tqxkf g"qxgtenii wkf epeg"kp"vj g"etge"qh"i gpgteniredqtevqt { "uchgv(0Gcej " redqtevqt { "j cu"ur gektke"tgs wktgo gpvu"deugf "qp"j e| etf u"euuqekevgf "y kij "vj g"vcum0

Cp{"s wguvkqpu"eqpegtpkpi "uchgv{"uj qwrf "dg"f ktgevgf "vq"yj g"J Y EQG"F ktgevqt "qh"Uchgv{ "qt"Ncd"Uchgv{ "Eqqtf kpcvqtu0" Go gti gpe{"rj qpg"pwo dgtu"hqt"yj g"Ncd"Uchgv{ "Eqqtf kpcvqtu."Ekxkrl'cpf "Eqcuvcn'Gpi kpggtkpi "r gtuqppgn"yj g"I ckpguxkng"Hktg" F gr ctvo gpv'cpf "vj g"WHRqrkeg"F gr ctvo gpv'y kni'dg"r tqo kpgpvn{ "f kur nc{ gf "cv'ugxgtcni'r qkpwi'kp"yj g"ncd"ctgcu0

Tguqwtegu<

Wpksgtukv{ "qh'Hrqtkf c'Gpxktqpo gpvcn'J gcnij "("Uchgv{ "/"j wr u<li y y y @j u0vln@f wl
J gtdgtv'Y gtvj gko "Eqmgi g'qh'Gpi kpggtkpi "Uchgv{ "Ohhkeg"/"j wr u<li y y y @pi 0vln@f wluchgv{ 1}

UCHGV| 'TGNCVGF'VGNGRJ QPG'PWO DGTU

Lco gu'Hrggwy qqf .'Fktgevqt 'qh'Uchgv{ .'J gt dgt v'Y gt vj gko 'Eqngi g'qh'Gpi kpggt kpi *574+4: 6/9: 76

*****574+'': 68/5748

GUUKG'Qltkeg

*574+'5; 4/; 759

Wpksgtuks{ 'J gcnyj 'Ugt xlegu

*574+5; 4/3383

Creej we'Eqwpv('O gpwedJ genj 'Etkki'Nkpg

*574+486/89::

Gpxktqpo gpvcnlJ gcnj '('Uchgv{

*****574+'5; 4/37; 3

J c | ctf qwu'Y cuwg'O cpci go gpv

*574+'5; 4/: 622

Y at mgt uø Eqorgpuc vlap

*574+'5; 4/6; 62

Wplxgtulx{ 'Rqrleg'F gr ct vo gpv'/'*P qp/Go gt i gpe{+

*574+5; 4/3333

Wplkgtuky 'Ranleg'F gr ct vo gpv'/'; 33

I cloguxkng'Hktg'Fgrctvo gpv'/';33

EJ CRVGT'8<'EQO RWGT'UWRRQTV

Vj g"f gr ctvo gpv'qh'Ekxki'cpf 'Eqcuvcn'Gpi kpggtkpi 'ku'pqv'tgur qpukdng'hqt'o ckpvckpkpi 'qt'tgr cktkpi 'cp{ 'r gtuqpcm{ "qy pgf 'eqo r wgtu0'Ki'uwf gpwi'j cxg''c'r tqdngo 'y kj ''y gkt''÷r gtuqpcnø'eqo r wgtu.''y g{ 'ecp'tgegkxg'j gnr 'htqo ''y g'' Wpkxgtuk{øu'öJ GNR'F GUMö0'Vj g"J gnr 'F guniecp'tdg'eqpvcevgf 'd{ 'ecmkpi '5; 4/J GNR'O'Vj g"J gnr 'F guniuchh'y kni'vt {''vq'' cpuy gt''cp{ ''s wgukqpu''qt'j gnr 'y kj ''cp{ ''r tqdngo 0'Ki'yj g{ ''o wnv'nqqm'cv'{qwt''o cej kpg.''{qwy kni'pggf ''vq'o cng''cp'' crrqkpvo gpv'vq''cng'kv'vq''y go 0'Hqt'kphqto cwqp''cdqww'eqo r wkpi 'ugtxkegu''cv'\WH''ceeguu''yj ku'\wtn'' i wr uslikovn'off wli gnr f gumi

EJ CRVGT'9<0 KJEGNNCP GQWUVQRKEU

MG['RQNKE[

Mg{u'y kn'idg'cuuki pgf ''q'cm'pgy 'heewn\{ .'unchh ''xkukkpi ''r tqhguuqtu''qt''uej qretu''cpf ''i tef wevg''uwf gpvu''chvgt''c'heewn\{ ''qt'' ef o kpkntevkxg''uki pewtg''j cu''dggp''qdvckpgf 0

C"eqo r ngvgf "Mg{"cpf 'Dwkrf kpi 'T gs wguv'hqto '*hqwpf "qp"vj g'GUUKG'y gdukg+"o wuv'dg'uwdo kwgf 'vq'vj g't gegr wqpkuv' nqecygf 'kp'587"Y gkr0C'ng{'y kni'y gp'dg'i kxgp'vq'vj g't gs wguvqt0

Ukpeg"kv'ku'f khhkewn'hqt''y g''ng{ 'eqqtf kpc'qt''\q''\tcem'f qy p''wpf gti tcf wc'yg''uwf gpuu'cpf 'r quv'f qe''uwf gpvu''mg{ u'ctg" tctgn('tgwtpgf 'cpf 'ctg''wwcm('r cuugf 'qp''\q''y g''pgzv'i tqwr ''qh''uwf gpvu+:'xkukkpi ''uej qrctu'cpf 'r tqhguuqtu.''mg{ u'hqt''y gug'' i tqwr u'y km'qpn('dg''cuuki pgf ''\q''y g''hcewn{ 'o go dgt''qt''y g''enwd lqti cpk cvkqp''ur qpuqt''cpf 'j gluj g'y km'dg''tgur qpukdrg'hqt'' o ckpvckpkpi ''y ku''ng{ ''kpxgpvqt { ''cpf 'tgwtpkpi ''y g''ng{ u''q''y g''eqqtf kpcvqt''qpeg''uwttgpf gtgf ''d{ ''y g''j qrf gt0}

Uwf gpwl'ctg'tgs wktgf '\q'uwttgpf gt'\j gkt'mg{u'r tkqt'\q'\j g'eqo o gpego gpv'egtgo qp{0C'j qnf 'y kn'dg'r reegf 'qp'\j g' i tcf wc\kpi '\uwf gp\u'\cequpv'\uprguu'\j g''ng{ 'ku'tgwtpgf 'r tkqt'\q'eqo o gpego gp\0'Kp'\j g'ecug'\j cv'c'uwf gpv\y kn'dg'' eqp\uprbwkpi '\uprbut' hrtvj gt'i tcf wc\g'y qtn'qt'cu'c'r quv'f qe.'j gluj g'uj qwnf 'o ggv\y kj '\j g''ng{ 'eqqtf kpc\qt'\q'\uprbphqto 'j gt ij ko '\j cv' y ku'ku'\y g'ecug\0Ki\j g'\uwf gp\und ku'c'r quv'f qe.'j kulj gt''ng{ 'y kn'dg'tgcuuki pgf '\q'\j g'\uwf gp\und ki\uprbphqto 'j uwr gtxkuqt\0

O CKN

Vj g'F gr ctvo gpvcn'o ckrlku'r kengf "wr "cv'cr r tqzko cvgn("; ⊲7"CO 0'Ki"{qw'ctg"o ckrlpi "cp{yi kpi ."{qw'o wuv'kpenwf g" yi g'r tqlgev'ceeqwpv'pwo dgt0FQ'PQV'WUG'VJ G'WPKXGTUKV['O CKN'UGTXKEG'HQT'RGTUQPCN'WUG0

Wpkxgtuky 'tgi wrcvkqpu'rtqj kdk'r gtuqpcn'o ckn'\q'dg'rtqeguugf 'htqo 'f grct vo gpvcn'qkheguOKp'cf f kkqp. 'f q'pqv'wug' y g'Ekxkn'cpf 'Eqcuvcn'Gpi kpggtkpi 'F grct vo gpv'cf f tguu'qp'r gtuqpcn'o ckn'*g0 0'tgeqtf 'enxdu. 'ej cti g'ectf u. 'dcpn'ceeqwpvu.'' gveOtOKG'{qw'j cxg'r gtuqpcn'ugn'uvco r gf 'o ckn''{qw'ecp'\cng'k\'vq'y g'o ckp'qhhkeg. 'cpf 'kv'y km'dg'o ckgf 'hqt''{qw0}

F wg"vq"yi g"neti g"pwo dgt"qhi'i tef wevg"uwf gpwu."kpf kxkf wenio ckndqzgu'ecppqv'dg"r tqxkf gf 0J qy gxgt."y g"f q"r tqxkf g" o ckndqzgu'd{ "ctgcó" "uxtwewtgu. "tcpur qtvcvkqp. "gve0+"Cp{ "WH'o ckniy kmidg"r megf "kp"yi gug"dqzgu0Dg"uwtg"vq"ej genilkv"qhvgp0' Kii'{qw'ej cpi g"{qwt"r tqi tco "vq"c"f khhgtgpv'ctgc."dg"uwtg"vq"eqpvcev'yi g"uvchhl'kp"yi g"I TCE"uq"yi cv'yi g"i tcf wevg"uwxf gpv'hkuv'ecp" dg"eqttgevgf "cpf" "{qwt"o ckniy kmidg"r megf "kp"yi g"eqttgev'ctgc"o ckndqz0

CWF KO IX HUWCN'GS WKRO GP V

Vj g'Ekxkrl'Gpi kpggtkpi 'O clqt'kp''y g'Ekxkrl'cpf 'Eqcuverl'Gpi kpggtkpi 'F gr ctvo gpv'j cu'ugxgterlr kgegu'qh'ewf kq kxkrverl' gs wkr o gpv'y j kej 'ecp''dg''ej gengf ''qww'hqt''r tgugpvevkqpu''vq''encuugu. 'hkpcrlf ghgpug. ''gve0''dww'pqv'hqt''r gtuqperl'wug0

K6'{qw'y kuj "vq"tgugtxg"cp"qxgtj gcf "rtqlgevqt."unkf g"rtqlgevqt."qt"VX"y kuj "XET."ugg"vj g"EEG"F grctvo gpv'Rtqi tco "Cuukuvcpv'kp"vj g"o ckp"qhhkeg0'Ukpeg"vj ku"gs wkr o gpv'ku"kp"j ki j "f go cpf."kv'ku"uvtqpi n{ 'tgeqo o gpf gf "vj cv"{qw'o cng"{qwt" tgugtxcvkqpu"ugxgtcn"f c{u"kp"cf xcpeg0}

EQPHGTGPEG'TQQO 'TGUGTXCVKQPU

Uwf gpw'y j q'y qwf ''hng''q'wkrk g''y g''eqphgtgpeg''tqqo ''o ww'ugg''y g''tgegr wkqpkw'nqecvgf ''kp''587''Y gkri'J cm''q'' tgugtxg''y g''ur ceg''cpf ''ej gem'hqt''cxckrcdkrk (0

Tgxkugf ": 09047